

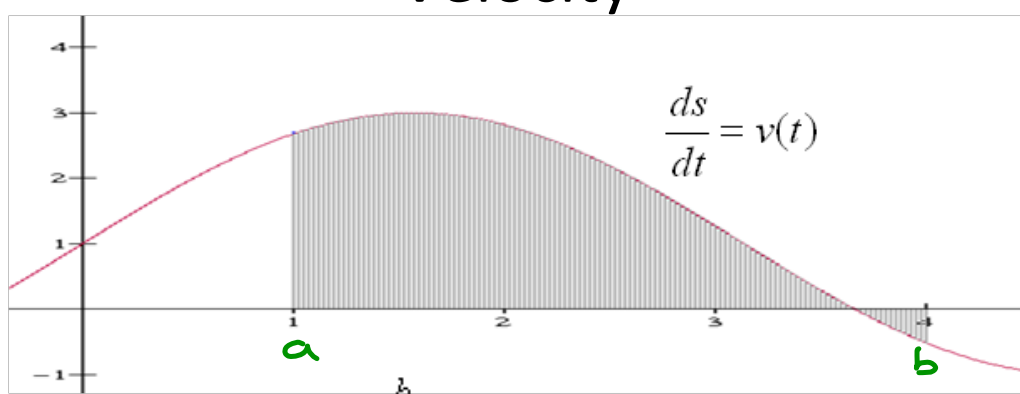
7-1 Integral as Net Change

Learning Targets

Given a differential equation, I can use integration to find a net change in a real world situation.

Given a differential equation and a starting value, I can use integration to find the ending value in a real world situation.

Velocity



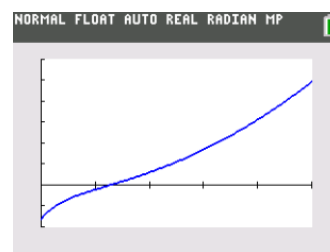
- What does $\int_a^b v(t) dt$ mean?

net change in area from time = a to time = b
 (displacement) position

- If $s(a)=12$ and $\int_a^b v(t) dt = 9$, what is $s(b)$?
 $12 + 9 = 21$
 final position = initial position + displacement

Example 1: $\frac{ds}{dt} = v(t) = t^2 - \frac{8}{(t+1)^2} \frac{\text{cm}}{\text{sec}}$

is a velocity function on $0 \leq t \leq 5$



- Graph the velocity for

- Describe the motion.

- What is the particle's position at time $t=1$ sec and

at $t=5$ sec if $s(0)=9$? $\int_0^1 (t^2 - \frac{8}{(t+1)^2}) dt = -3.667$
 $9 - 3.667 = 5.333 \text{ cm}$

$\int_0^5 v(t) dt = 35$ $9 + 35 = 44 \text{ cm}$

- What was the total distance travelled from $t=0$ to $t=5$? $\int_0^5 |v(t)| dt = 42.587 \text{ cm}$

Integral as a Net Change

If f is a continuous and differentiable function over $[a, b]$, then

$$f(b) = f(a) + \int_a^b f'(x) dx$$

final position = initial position + displacement

And the integral $\int_a^b f'(x) dx$ tells you how much the function has changed from a to b .

Example 2:

$f'(x)$ is defined on $[-6, 7]$

$f(0) = 5$

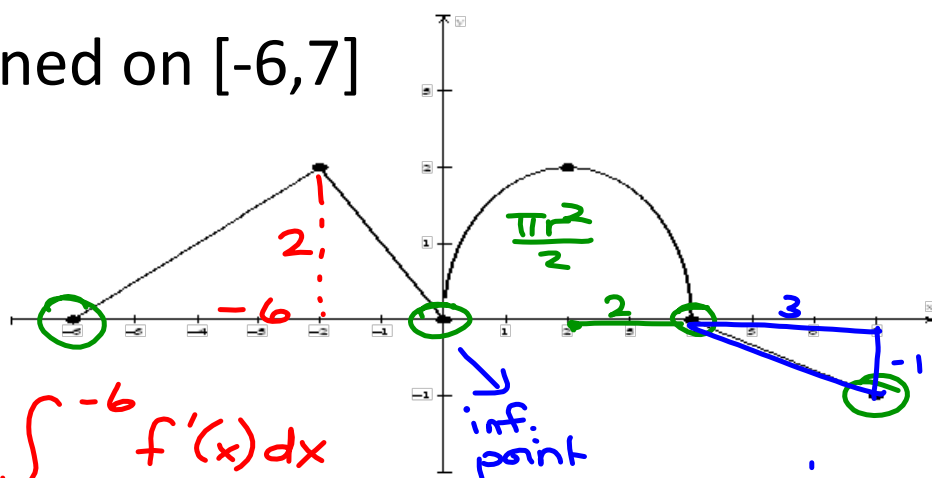
Candidates:

$-6, 4, 7$

$$\begin{aligned} -6: & 5 + \int_0^{-6} f'(x) dx \\ & 5 + -6 = \textcircled{-1} \end{aligned}$$

$$\begin{aligned} 4: & 5 + \int_0^4 f'(x) dx \\ & 5 + 2\pi \\ & = 11.28 \end{aligned}$$

$$\begin{aligned} 7: & 5 + \int_0^7 f'(x) dx \\ & 5 + 2\pi + -1.5 \\ & 9.78 \end{aligned}$$



- Find the absolute maximum of $f(x)$ on $[-6, 7]$.
11.28
- Find the absolute minimum of $f(x)$ on $[-6, 7]$.
-1

Homework

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